HOMEWORK 3 - MATH 110 DUE DATE: Friday, September 27 INSTRUCTOR: George Voutsadakis

Read each problem very carefully before starting to solve it. Each problem is worth 3 points. It is necessary to show your work. Correct answers without explanations are worth 0 points.

GOOD LUCK!!

- 1. What is the smallest natural number n, greater than 1, for which $(1 \times 2 \times 3 \times \ldots \times n) + 1$ is not prime?
- 2. Is it possible for an extremely large prime to be expressed as a large integer raised to a very large power? Explain.
- 3. Are there infinitely many natural numbers that are not prime? If so, prove it.
- 4. Today is Saturday. What day of the week will it be in 3,724 days? What day of the week will it be in 365 days?
- 5. Look up your bank code on your check. Verify that it is a valid bank code.
- 6. Compute $5^{600} \pmod{7}$.