

## EXAM 2 - MATH 140

DUE DATE: Tuesday, October 19

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Read each problem very carefully before starting to solve it. Each question is worth 3 points. It is necessary to show your work. Correct answers without explanations are worth 0 points.

GOOD LUCK!!

1. Graph the piece-wise defined function  $f(x) = \begin{cases} |x-1|, & \text{if } x \leq 3 \\ -(x-4)^2 + 2, & \text{if } x > 3 \end{cases}$  making sure to label some of the critical points in your graph. Then find the domain and the range of  $f$ .
2. Use the sign table method to make a rough sketch of the graph of the function  $f(x) = x^4 - 7x^3 - 8x^2$ . Then find the solution set of the inequality  $x^4 - 7x^3 - 8x^2 < 0$ .
3. Find the domain, the intercepts, the asymptotes, create the sign table and then roughly sketch the graph of the function  $f(x) = \frac{2x+14}{x^2-2x-3}$ . Then find the solution set of the rational inequality  $\frac{5}{x-3} - \frac{3}{x+1} \leq 0$ .
4. An open box with a square base is required to have a volume of 10 cubic feet. Express the amount  $A$  of the material used to make such a box as a function of the length  $x$  of the side of the square base.
5. Let  $f(x) = \frac{x-1}{x+3}$  and  $g(x) = \frac{2}{x+7}$ . Find a formula for the composite  $f \circ g$  and then determine its domain.
6. The function  $f(x) = \frac{3x+4}{2x-5}$ ,  $x \neq \frac{5}{2}$  is one-to-one. Find its inverse and then determine the domain and the range of  $f$ .