PRACTICE EXAM 1 - MATH 151

DATE: Friday, September 21

INSTRUCTOR: George Voutsadakis

Read each problem very carefully before starting to solve it. Each question is worth 5 points. It is necessary to show your work. Correct answers without explanations are worth 0 points.

GOOD LUCK!!

- 1. (a) Starting from the graph of $f(x) = \sqrt{x}$ give the step-by-step transformations that need to be followed to graph the function $g(x) = \sqrt{4-2x} 6$. (You do not need to do the actual graphing.) (3 points)
 - (b) Which function g(x) has the same graph as the graph of $f(x) = \frac{1}{x}$ after it is shifted two points down, reflected with respect to the x-axis, stretched vertically by a factor of 3 and moved right by 5 points (in the given order)? Present carefully all intermediate steps. (2 points)
- 2. Suppose that $f(x) = \frac{3}{x-1}$ and $g(x) = \sqrt{x+3}$.
 - (a) Find the domains Dom(f) and Dom(g). (1 point)
 - (b) Find a formula for $(g \circ f)(x)$ and simplify. (2 points)
 - (c) Find the domain of $g \circ f$. (2 points)
- 3. (a) Graph the piece-wise defined function $f(x) = \begin{cases} (x+1)^3, & \text{if } x < -1 \\ -x^2 + 1, & \text{if } -1 \le x < 2 \end{cases}$ (2 points) Find the limits $\lim_{x \to -1} f(x)$ and $\lim_{x \to 2} f(x)$ (1 point).
 - (b) Suppose that $\frac{1}{2}x+1 \le f(x) \le x^2-4x+6$ for all x. Find the $\lim_{x\to 2} f(x)$. Justify your answer. (2 points)
- 4. Find the following limits:
 - (a) $\lim_{x\to 1} \frac{x^2+4x-5}{-x^2+4x-3}$ (2 points)
 - (b) $\lim_{x\to 11} \frac{11-x}{\sqrt{x-2}-3}$ (2 points)
 - (c) $\lim_{t\to 0} \left(\frac{1}{t} + \frac{1}{t^2-t}\right)$ (1 point)
- 5. Find the following trigonometric limits:
 - (a) $\lim_{\theta \to 0} \frac{\sin 3\theta}{\sin 7\theta}$ (2 point)
 - (b) $\lim_{t\to 0} \frac{5t^2}{\sin^2 2t}$ (3 points)
- 6. (a) Complete the formal definition: "A function f(x) is continuous at x = a if ...". (2 points)
 - (b) Consider the function $g(x) = \begin{cases} \frac{x^2 x 6}{x^2 + x 2}, & \text{if } x \neq -2, 1 \\ a, & \text{if } x = -2 \end{cases}$ Find the value of a (if any) so that g be continuous at x = -2 (2 points). Find the value of b (if any) so that g be continuous at x = 1 (1 point).

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