EXAM 1 - MATH 111 YOUR NAME:

Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

- 1. The enrollment N in millions of students t years since 1965 in US public high schools is given by $N = -0.02t^2 + 0.44t + 11.65$. The model is applicable from 1965 to 1985.
 - (a) Calculate N(7) and explain in practical terms what it means.
 - (b) In what year was the enrollment the largest? What was that largest enrollment?
 - (c) Find the average yearly rate of change in enrollment from 1965 to 1985.
 - (d) Graph N vs. t by appropriately adjusting your window. Explain in a short sentence your window choices.

- 2. The yearly profit P for a widget producer is a function of the number n of widgets sold. The formula is $P = -180 + 100n 4n^2$, where P is measured in thousands of dollars, n is measured in thousands of widgets and the formula is valid up to a level of 20 thousand widgets sold.
 - (a) Make a graph of P vs. n.

(b) Calculate P(0) and explain in practical terms what your answer means.

(c) What profit will the producer make if 15 thousand widgets are sold?

(d) Approximate the break-even point for this widget producer.

(e) What is the largest profit possible?

- 3. The relationship between the distance d in miles that you can travel without stopping for gas, the number of gallons g of gasoline in your tank and the gas mileage m in miles per gallon that your car gets is given by d = gm.
 - (a) How far can you drive if you have 12 gallons of gas in your tank and your car gets 24 miles per gallon?
 - (b) Solve the given equation for m. Explain in everyday terms what your new equation means.
 - (c) Use the new equation to determine the gas mileage of your car if you can drive 335 miles on a full 13-gallon tank of gas.
 - (d) A Detroit engineer wants to be sure that the car she is designing can go 425 miles on a full tank of gas, and she must design a gas tank to ensure that. She does not know yet what gas mileage this new model-car will get and so she decides to make a graph of the size of the gas tank as a function of the mileage. Make the graph that the engineer made.

- 4. Solve the following inequalities and make a graph of the solution sets.
 - (a) $-x^2 + 5x + 14 < 0$

(b)
$$\frac{x+2}{x^2+2x-15} \ge 0$$

- 5. We want to form a rectangular pen of area 100 square feet. One side of the pen is to be formed by an existing building and the other three sides by a fence. Let W be the length in feet of the sides of the rectangle perpendicular to the building and L the length in feet of the other side.
 - (a) Find a formula for the total amount of fence needed as a function of both W and L.
 - (b) Express as an equation involving W and L the requirement that the total area formed be 100 square feet.
 - (c) Solve the equation you found in Part (b) for L.
 - (d) Use your answers in Parts (a) and (c) to find a formula for F, the total amount, in feet, of fence needed as a function of W alone.
 - (e) Make a graph F vs. W (and adjust your window).
 - (f) Determine the dimensions of the rectangle that requires the minimum amount of fence.