Read each problem very carefully before starting to solve it. Each problem is worth 10 points. It is necessary to show all your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Find the following integrals:
(a) $\int \frac{(3 x-1)(2 x-7)}{x} d x=$
(b) $\int \frac{1}{x}\left(2019-2019 x e^{2019 x}\right) d x=$
2. Find the area enclosed by the graphs of the functions $f(x)=x^{3}+2 x$ and $g(x)=3 x^{2}$.
3. Your uncle invested in 2010 in a real estate deal originally worth $\$ 20,000$ and growing at the rate of $400 e^{0.05 t}$ dollars per year, where $t$ is the number of years since the investment was made.
(a) Find a formula for the value of the investment $t$ years after 2010 (please, simplify to prepare to answer Part (b) more comfortably).
(b) When will the investment be worth $\$ 52,000$ ?
4. Find the average value of the function $f(x)=6 x^{2}-4 e^{2 x}$ from $x=0$ to $x=2$.
5. Evaluate the following integrals
(a) $\int \sqrt[5]{3 x^{2}-6 x}(x-1) d x$
(b) $\int_{1}^{3} \frac{e^{1 / x}}{x^{2}} d x$
