

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. (a) Solve the exponential equation

$$(3^x)^{x^2} = 27^{3x}.$$

- (b) Solve the logarithmic equation

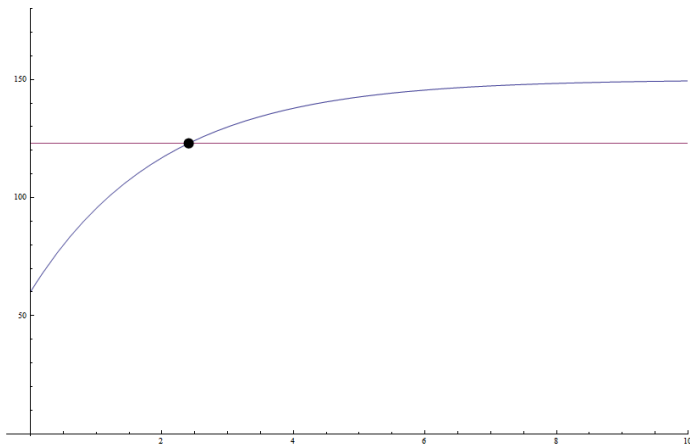
$$\log_{2019} x + \log_{2019} (x - 1) = \log_{2019} (x + 8).$$

2. The population in the wild of a certain species  $t$  years from now is modeled by the equation

$$P(t) = 30(5 - 3e^{-\frac{1}{2}t}) \quad (\text{in thousands of individuals}).$$

(a) How many individuals are currently in the population (show all steps; do not just read from the graph)?

(b) When will the population reach 123,000 individuals?



(c) How fast will the population be changing in 2 years time?

3. Your grandparents were very forward looking and pro-education and deposited in 1978 a certain capital at an account yielding 4% compounded monthly so that in 2018 the account would have \$60,000.

Your parents took that amount in 2018 and put it in a new account yielding 3% compounded semiannually so that you and your siblings may use it for the education of your own kids in the future.

- (a) Find how much your grandparents deposited in 1978.

- (b) Find in how many years from now the account your parents created will have \$90,000 in it.