

YOUR NAME: \_\_\_\_\_

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Read each problem **very carefully** before starting to solve it. Each problem is worth 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Find  $(f^{-1})'(2)$  if  $f(x) = \sqrt{2x^4 + x^2 + 1}, x \geq 0$ .

2. Find  $\frac{dy}{dx}$  if  $x^y = y^x$ .

3. (a) Use the derivatives of exponential functions to show that  $(\operatorname{csch} x)' = -\operatorname{csch} x \coth x$ .

(b) Find the derivative  $f'(x)$  if  $f(x) = e^{2x} \operatorname{csch}(5x)$ .

4. Find the critical points of the function  $f(x) = \sqrt[5]{x^3 - 12x}$