

YOUR NAME: \_\_\_\_\_

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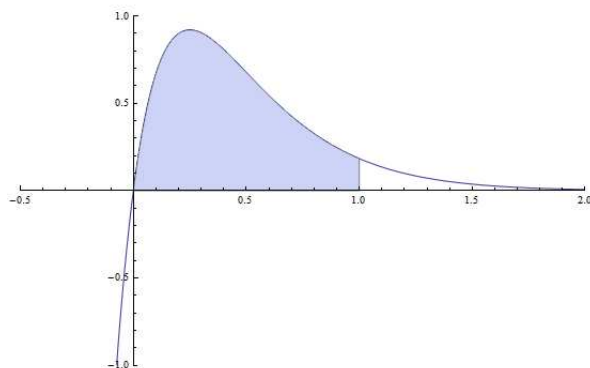
Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. Use substitution to find the indefinite integrals:

(a)  $\int x^2 e^{x^3} dx$

(b)  $\int \sqrt{\ln x} \frac{1}{x} dx$

2. Use the by-parts method to evaluate the definite integral  $\int_0^1 10xe^{-4x} dx$



3. Evaluate the improper integral  $\int_5^{\infty} \frac{1}{(x-4)^5} dx$

4. Solve the differential equation  $y^4 y' = 3x^2$  subject to  $y(0) = 1$ .

5. Solve the differential equation  $y' = xy - 5x$ , with  $y < 5$ , subject to  $y(0) = 4$ .