Friday, February 7 George Voutsadakis

Read each problem **very carefully** before starting to solve it. Each problem is worth 10 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

- 1. (a) A line  $\ell$  has equation 3x + 5y = 7. A line  $\ell'$  passes through the points (1, -21) and (10, -36). Show all your work in answering the following questions.
  - (i) Find the slope of  $\ell$ .

(ii) Find the slope of  $\ell'$ .

(iii) Tell whether  $\ell$  and  $\ell'$  are parallel, perpendicular or neither and explain.

(b) Find the domain of the function  $f(x) = \frac{x+7}{3x^3+2x^2-5x}$ .

- 2. A certain manufacturer has fixed costs \$3200 and variable costs \$100 per each item produced. Suppose its revenue function is  $R(x) = -2x^2 + 300x$ , where x is the number of items produced and sold.
  - (a) Find the cost function C(x).
  - (b) Find the break-even point(s).

- (c) Find an equation for the profit function P(x).
- (d) Find the number of items that need to be produced to maximize the profit. Explain your work.

3. Compute the difference quotient of  $f(x) = x^2 + 7x$  at x and simplify.

4. The position function of a moving object at time t in seconds is given by  $s(t) = \sqrt{2t-1}$  in meters. Find the instantaneous velocity of the object at time t = 5 seconds.

5. Consider the piece-wise defined function

$$f(x) = \begin{cases} \frac{x^2 - 7x + 10}{x - 2}, & \text{if } x < 2\\ -3, & \text{if } x = 2\\ \frac{\frac{1}{x} - \frac{1}{2}}{x - 2}, & \text{if } x > 2 \end{cases}$$

Calculate the following:

f(2) = $\lim_{x \to 2^{-}} f(x) =$ 

 ${\lim_{x\to 2^+}}f(x) =$ 

$$\lim_{x \to 2} f(x) =$$

State the type of continuity of f at x = 2, if any.