Read each problem **very carefully** before starting to solve it and do only what is asked. Each problem is worth around 5 points. It is necessary to show **all** your work. Correct answers without explanations are worth 0 points. GOOD LUCK!!

1. [4 points] Solve the initial value problem

 $y'' + 10y' + 26y = 0, \quad y(0) = 5, \ y'(0) = 12.$ 

2. [4 points] Solve the initial value problem

$$y'' + 14y' + 49y = 0, \quad y(0) = -3, \ y'(0) = 63.$$

3. [6 points] Consider the differential equation

$$t^{3}y'' - y' - (6t - 3t^{-1})y = 0.$$

Suppose we know that  $y_1(t) = t^3$  is a solution. Find the first order differential equation that results from applying the method of reduction of order. (You do not have to solve the equation.)